4 Enhancements and Other Odd-ities

• Learning,

$$J_{i,j}(new) = \beta J_{i,j}(old) + \alpha s_i(p) s_j(p),$$
 (handwriting recognition, ...)

- More states for neuron: color picture memory, image processing.
- **feedforward networks**, layered neuron only communicate through the next layer (perceptron).
- An NN has been shown to be capable of universal computation (Turing machine).
- Seem capable of massively parallel processing.

- 3 Examples
- Letter Recognition —

2.3 Limitations

- $N \text{ spins} \to N^2 \text{ different } J_{i,j}$.
- We'd think $N^2/N=N$ different patterns could be held.
- Actually, $\sim 0.14N$.
- The **Hamming distance**, energy minima, and interference.

$$\Delta_{m,n} = \frac{1}{N} \sum_{i} [s_i(m) - s_i(n)]^2$$

• Still fairly resilient, content addressable memory...

2.2 Storing a Pattern

- ullet The energy landscape, J, of the system defines how a memory is "stored" in the neural net.
- A very rudimentary definition is

$$J_{i,j} = s_i(m)s_j(m)$$

where $s_i(m)$ denotes the configuration of spin i in pattern m.

- Effectively we are defining the lowest energy state of the system as our pattern.
- We are not limited to one pattern,

$$J_{i,j} = \frac{1}{M} \sum_{m} s_i(m) s_j(m).$$

But we are limited...

2 Application

- Memory via a Neural Net —
- In order to recall a pattern in a neural net memory, we require that the spin directions change with time such that the spin configuration ends up in a desired state.

The MC Approach:

- 1. Start with a particular configuration of the entire network.
- 2. Choose a spin and calculate the energy required to flip it, ΔE , from our relation for E.
- 3. If $\Delta E_{flip} < 0$, flip it.
- 4. If $\Delta E_{flip} \geq$ 0, don't flip it.

- The connections in a real neural network are **not symmetric**: $(i \rightarrow j) \neq (j \rightarrow i)$; but, hell, what if they were? (Question: Why is this asymmetry important?)
- ⇒ We could use some Statistical Mechanics!
- ullet E gives us a way to model a neural net via **Monte Carlo** by seeking a lower energy state,

only we define what the lowest energy state is through J (more on this later).

 \Rightarrow Apply these assumptions to the application of **memory**.

1.4 A Modified Ising Model

- In the typical Ising Model, the effect of a spin on its neighbors was through the exchange energy. (remember, magnet)
- Similarly here, but we must consider every pair of spins.
- We define the effective energy of the neural network as

$$E = -\sum_{i,j} J_{i,j} s_i s_j,$$

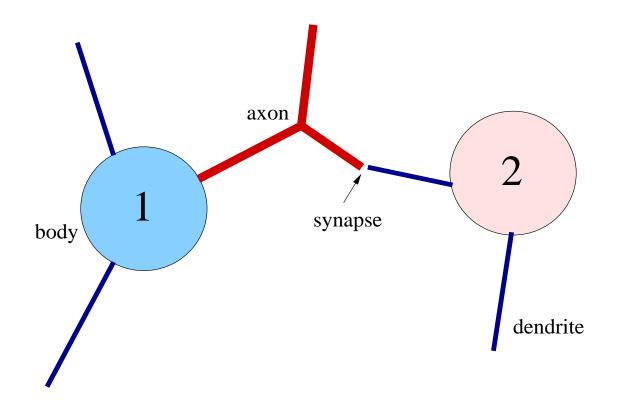
where $J_{i,j}$ is the interaction energy: describes the influence of neuron i on the firing rate of neuron j.

 $\sum_{j} J_{i,j} s_{j}$ determines the firing rate, ie spin, of neuron i. (Think of J as the effective field (eg magnetic) established by its neighbor's spins.)

- A Physicist's Guide to the Brain 2 –
- 1.3 The Ising Model! (What else?)
 - **Discrete** matrix of neurons with two states: firing or not firing (up spin, down spin ... sound familiar?)
 - With Long-Range interactions. What are interactions?
 - Assume no time-dependence of synaptic signals. (ok, biological evidence for nonsynchronousness ... maybe)

1.2 Neural Networks

- Associative Memory (classification, reconstruction, training, learning).
- Understanding how a Neural Network = brain is a big (and cool) problem. (AI, pattern recognition, memory).



- Neuron's state: firing or not firing; a function of its inputs.
- Connections are not limited to neighboring neurons, but can extend to neurons in remote areas of the brain.
- Many Neurons = Neural Network =
 Brain = Remarkable

1 Overview

- A Physicist's Guide to the Brain —
- 1.1 First, a pinch of biology: Neurons
 - \bullet The brain is made up of $\sim 10^{12}$ neurons.
 - Neurons communicate via electrical and chemical signals carried by dendrites and axons.
 - \bullet Very interconnected, inputs from $\sim 10^4$ other neurons. Not two-way.
 - Neurons fire as a function of their inputs
 (high, roughly periodic rate, or much lower
 rate). (>>inhibitory and exhibitory synapses)

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Computer Simulations of Neural Networks

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